

RESEARCH ARTICLE

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Added value of far-infrared radiometry for remote sensing of ice clouds

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Key Points:

- Ice cloud remote sensing would be greatly improved by adding far-infrared channels to existing midinfrared spaceborne radiometers
- Far-infrared radiometry is well suited to study ice clouds in the polar regions and upper troposphere
- Using far-infrared radiometry extends current infrared capabilities to large optical thickness and large cloud particles

Supporting Information:

- Supporting Information S1
- Table S1
- Table S2
- Table S3

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Abstract Several cloud retrieval algorithms based on satellite observations in the infrared have been developed in the last decades. However, these observations only cover the midinfrared (MIR, $\lambda < 15 \mu\text{m}$) part of the spectrum, and none are available in the far-infrared (FIR, $\lambda \geq 15 \mu\text{m}$). Using the optimal estimation method, we show that adding a few FIR channels to existing spaceborne radiometers would significantly improve their ability to retrieve ice cloud radiative properties. For clouds encountered in the polar regions and the upper troposphere, where the atmosphere is sufficiently transparent in the FIR, using FIR channels would reduce by more than 50% the uncertainties on retrieved values of optical thickness, effective particle diameter, and cloud top altitude. Notably, this would extend the range of applicability of current retrieval methods to the polar regions and to clouds with large optical thickness, where MIR algorithms perform poorly. The high performance of solar reflection-based algorithms would thus be reached in nighttime conditions. Since the sensitivity of ice cloud thermal emission to effective particle diameter is approximately 5 times larger in the FIR than in the MIR, using FIR observations is a promising venue for studying ice cloud microphysics and precipitation processes. This is highly relevant for cirrus clouds and convective towers. This is also essential to study precipitation in the driest regions of the atmosphere, where strong feedbacks are at play between clouds and water vapor. The deployment in the near future of a FIR spaceborne radiometer is technologically feasible and should be strongly supported.

Plain Language Summary The size of ice cloud particles can be estimated from space by measuring the infrared emission of ice clouds. However, this method no longer works when clouds are too thick or when particles are too large, although such clouds are encountered in many regions of the Earth and are critical for the Earth's climate. Using new sensors that measure cloud emission at longer wavelengths, in the so-called far-infrared region, would extend the potential of satellite observations to thick clouds, to clouds made of larger particles, and to clouds found in the polar regions which are very poorly known. These new sensors have become available in the last years, but none is deployed in space so far. We show that a satellite equipped with a few channels in the far-infrared would greatly increase our capacity to observe ice clouds. This is promising for our understanding of cloud microphysics and precipitation in general, and for studying the water cycle in the polar regions in particular. For these reasons, it is highly recommended to deploy a far-infrared radiometer in space.

1. Introduction

Passive satellite observations have been extensively used to retrieve ice cloud radiative properties from space [e.g., Inoue, 1985; King *et al.*, 1992; Platnick *et al.*, 2003]. Generally, the quantities of interest are cloud optical thickness τ , effective particle diameter d_{eff} , and cloud boundaries altitudes. Contrary to active sensors such as CALIPSO [Winker *et al.*, 2003] and CloudSat [Stephens *et al.*, 2002] that only measure cross sections of cloud properties, passive sensors often allow imaging, which is very valuable to investigate the horizontal structure of clouds. A wide range of cloud retrieval methods have been developed, which generally take advantage of the strong variations of the ice refractive index throughout the solar spectrum and the infrared (IR) range. Methods based on solar reflection by clouds [e.g., Nakajima and King, 1990; King *et al.*, 2004] are efficient for optically thick clouds but limited to daytime conditions. Methods based on cloud IR signature are efficient for optically thinner clouds but are limited for optical thickness greater than about five [e.g., Iwabuchi *et al.*, 2014]. The IR methods have the advantage of being applicable indifferently for daytime and nighttime, which ensures consistency of the retrieval independently of solar illumination conditions. The original IR methods

were based on the split window technique [Inoue, 1985], which consists of measuring the atmosphere brightness temperature in two channels having distinct sensitivities to cloud properties. Those channels were generally chosen around 11 and 12 μm , ice being much less absorbing at 11 μm than at 12 μm . Later on, the addition of supplementary channels allowed to better constrain cloud properties [e.g., Baum *et al.*, 1994; Wei *et al.*, 2004; Yue and Liou, 2009; Wang *et al.*, 2011, 2013]. These methods are mostly based on look-up-table approaches, and retrievals are obtained by minimizing the root-mean-square deviation between the observations and tabulated values. More recently, a number of algorithms based on the optimal estimation method [Rodgers, 2000] were proposed [Cooper *et al.*, 2006; Iwabuchi *et al.*, 2014; Wang *et al.*, 2016a]. Such methods use all available channels to find the most likely state of a cloud. They also provide a rigorous estimation of the uncertainties associated to the retrievals.

The present study is based on the optimal estimation method and focuses on IR techniques, because those can be used at night. This is critical in the study of clouds during the polar night, a central topic of our research. Current IR retrieval methods are not appropriate in the study of optically thick clouds ($\tau > 10$) and clouds made of large particles ($d_{\text{eff}} \gtrsim 80 \mu\text{m}$) [Merrelli, 2012; Wang *et al.*, 2016b]. Such methods are also not suitable for the polar regions [Liu *et al.*, 2010], due to the low thermal contrast between the surface and clouds and because the low thermal emission of these cold areas generally results in a low signal-to-noise ratio. Those limitations are essentially due to the inherent single-scattering properties of ice particles in the midinfrared (MIR, $\lambda < 15 \mu\text{m}$), in which spaceborne radiometers such as Moderate Resolution Imaging Spectroradiometer (MODIS) [King *et al.*, 1992], Atmospheric Infrared Sounder (AIRS) [Aumann *et al.*, 2003], or Advanced Very High Resolution Radiometer (AVHRR) [Wang and Key, 2005] take their measurements. Yang *et al.* [2003] have shown that using well-chosen far-infrared (FIR, $\lambda \geq 15 \mu\text{m}$) hyperspectral channels could allow to retrieve effective particle diameter up to 100 μm , even in the case of optically thick clouds. This was confirmed by Merrelli and Turner [2013] who showed that the added value of FIR hyperspectral measurements is maximum for thick clouds and for large particles. FIR observations thus have the potential of observations performed in the solar spectrum, without their limitations.

Despite the acknowledged potential of FIR radiometry for retrieving ice cloud properties [e.g., Baran, 2007; Merrelli, 2012; Palchetti *et al.*, 2016a], no satellite observations of the Earth's atmosphere were performed in this spectral range since the Meteor satellite program in the late 1970s [Spankuch and Döhler, 1985]. The development of FIR spectrometers has been hindered for several reasons: (1) radiometric responsivity of existing sensors is much less in the FIR than in the MIR; (2) observations from the ground are in most locations useless since the atmosphere is essentially opaque in the FIR; (3) hyperspectral instruments in the MIR, such as AIRS or Infrared Atmospheric Sounding Interferometer (IASI) [Blumstein *et al.*, 2004], already contain much information about the atmosphere. There has been in the last decade a renewed interest for satellite missions in the FIR, though, mainly fostered by the availability of new technologies based on uncooled thermal sensors such as thermopiles [McCleese *et al.*, 2007], pyroelectrics [Palchetti *et al.*, 2006], and microbolometers [Ngo Phong *et al.*, 2015]. Such sensors, when coated with gold black, have sufficient sensitivities and are easier to deploy in space than cooled systems. The CLARREO project [Wielicki *et al.*, 2013], for instance, aims at measuring the spectrally resolved emission spectrum of Earth up to 100 μm . However, the current radiometric resolution in the FIR (10 K) is too low to observe clouds at short time scales. Instead, the instrument aims at providing very accurate large-scale averages of the Earth's radiative budget. The REFIR project [Palchetti *et al.*, 2006], which has been recently renamed FORUM [Palchetti *et al.*, 2016b], also intends to measure the FIR emission of the Earth, but is not specifically focused on ice cloud observation. These two projects, that are based on Fourier transform interferometry (FTIR), are ambitious and face budget issues, making their future still uncertain. Given that only a few channels (approximately five) contain the bulk of the information in most cloud retrieval algorithms [e.g., L'Ecuyer *et al.*, 2006; Wang *et al.*, 2016a], such high spectral resolution is not necessary for the specific application of cloud retrieval. As a consequence, an alternative resides in using narrow band radiometers rather than hyperspectral instruments. Such instruments can be more affordable, more robust, and less complex than FTIR systems that require high-precision optics. Radiometers essentially trade spectral resolution for radiometric resolution. This is the route chosen for the TICFIRE project (Thin Ice Clouds in the Far-InfraRed Experiment) [Blanchet *et al.*, 2011; Libois *et al.*, 2016a], which consists of a filter wheel IR imager with channels spanning the whole IR range from 8 to 50 μm . This mission, currently under review at the

Table 1. Cloud Characteristics for the Two Reference Cases

Quantity	Arctic Winter	Tropics
τ	1.0	1.0
d_{eff}	60 μm	60 μm
h_{bot}	5 km	14 km
h_{top}	6 km	15 km

Canadian Space Agency, will be dedicated to the observation of ice clouds in the polar regions and can be viewed as a FIR extension of MODIS.

The present study investigates the potential of FIR radiometry for ice cloud radiative properties retrieval. For this, the information content of FIR radiances for a variety of cloudy scenes

is estimated in the framework of the optimal estimation method. This work follows the method implemented by Wang *et al.* [2016a] and Iwabuchi *et al.* [2016] for MODIS observations but extends these studies to the case of FIR channels. Of particular importance is the estimation of effective particle diameter and the distinction between precipitating and nonprecipitating clouds. A special focus is thus put on uncertainties related to effective particle diameter retrievals and on the capacity to accurately estimate particle size for large particles. In the driest regions of the troposphere, that is, the polar regions and the near-tropopause, precipitation can result in the dehydration of the atmosphere [Curry *et al.*, 1995; Jensen *et al.*, 1996]. This can significantly alter the radiative budget, which is essentially driven by the natural greenhouse effect of water vapor [Blanchet and Girard, 1995]. Hence, cloud effective particle diameter is a critical quantity that affects the radiative budget of the Earth [e.g., Stephens *et al.*, 2002]. Improving existing cloud retrieval algorithms could complement active technologies which provide valuable insight into clouds microphysics, formation, and evolution [e.g., Austin *et al.*, 2009; Grenier *et al.*, 2009; Kayetha and Collins, 2016]. After providing a physical insight on the potential of FIR radiometry for studying ice clouds, section 2 provides details on the optimal estimation framework and on the synthetic satellite instrument used in this paper. In section 3, the information content of FIR observations is computed for two representative cases, namely a polar ice cloud and a tropical ice cloud. The added value of FIR is discussed in section 4, where leads for future work and recommendations for designing a spaceborne FIR radiometer are also given.

2. Motivation and Methods

In this section, the theoretical framework used to quantify the information content of FIR radiances for cloud properties retrieval is detailed. It is based on the optimal estimation method [Rodgers, 2000] and follows the approach of Wang *et al.* [2016a] and Iwabuchi *et al.* [2016]. Two types of ice clouds are studied in detail: a polar ice cloud and a tropical ice cloud. Since no spaceborne FIR radiometer exists so far, a synthetic instrument is used, whose characteristics are mainly based on those of the Far-Infrared Radiometer (FIRR) [Libois *et al.*, 2016a], which is a breadboard for the TICFIRE mission.

2.1. Atmospheric Profiles

The two types of clouds considered in this study are supposed to encompass most climatically relevant ice clouds encountered on Earth: a high-altitude ice cloud in a tropical atmosphere, which can be either a cirrus cloud or the anvil of a convective cloud, and a ubiquitous tropospheric ice cloud during Arctic winter. Both clouds are single layer and assumed homogeneous. The tropical cloud is located just beneath the tropical tropopause, between 14 and 15 km, while the polar cloud extends from 5 to 6 km altitudes consistent with the CALIPSO observations reported by Haladay and Stephens [2009] in the tropics and Grenier *et al.* [2009] in the Arctic. The atmosphere within the clouds is saturated. In the reference cases, those clouds have an optical thickness of 1.0 and an effective particle diameter of 60 μm , corresponding to a modified-gamma distribution with effective variance 0.1 [Petty and Huang, 2011] of severely roughened column aggregates [Yang *et al.*, 2013]. The same distribution is assumed in the Collection 6 MODIS cloud product [Holz *et al.*, 2016]. The characteristics of these reference cases are summarized in Table 1. The vertical profiles of temperature and water vapor mixing ratio for both atmospheres were computed from an average of 18 radiosondes taken from the IGRA database (<ftp://ftp.ncdc.noaa.gov/pub/data/igra/>). For the tropical profile, six radiosondes measured between 1 January 2015 and 1 November 2016 were randomly taken from each of the following stations: Abidjan, Corozal Oeste, and Piarco International Airport. The Arctic winter profile was computed from radio soundings measured in January or February of 2015 or 2016 at Alert, Eureka, and Resolute Bay. This profile is meant to be representative of typical winter conditions in the Canadian Archipelago. Both profiles are shown in Figure 1.

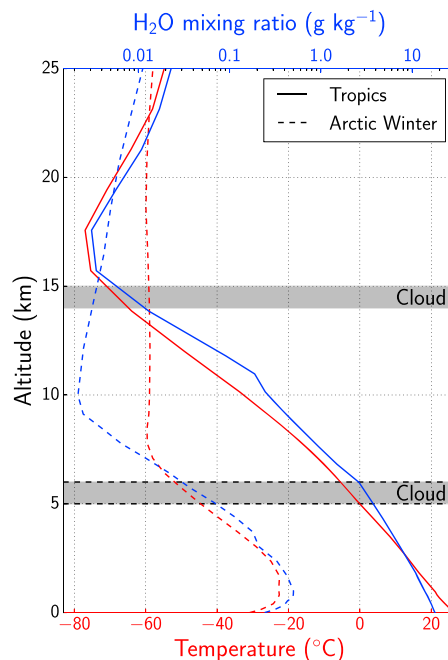


Figure 1. Atmospheric profiles for the Arctic winter and tropical reference cases. The positions of the ice clouds are indicated by the horizontal shaded area.

coated with gold black which has spectrally flat absorbance through the whole IR range [e.g., Ngo Phong *et al.*, 2015], and with the absence of significant spectral differences in the transmittance along the optical path. Such characteristics are expected for a grating-based or filter wheel-based radiometer. The radiometric resolution is defined in terms of NER rather than in terms of noise equivalent delta temperature (NEDT) to work at the sensor level. NEDT is helpful in comparing to actual temperature measurements, but it can be misleading as it depends on the temperature of the considered scene. Also, with this choice, increasing the number of bands clearly results in a decrease of the signal-to-noise ratio, which is easily understood because

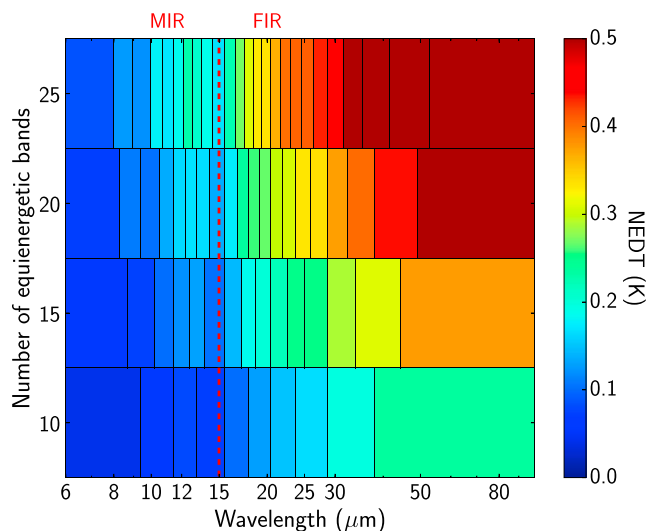


Figure 2. NEDT in each spectral channel as a function of total number of equienergetic bands, for a blackbody at 250 K. The NER is assumed spectrally constant and equals $0.01 \text{ W m}^{-2} \text{ sr}^{-1}$.

2.2. Instrument Characteristics

Contrary to the works of Wang *et al.* [2016a] and Iwabuchi *et al.* [2016] that were dedicated to MODIS, here we do not investigate the characteristics of a particular instrument but rather explore the potential of a synthetic spaceborne FIR radiometer. The instrument is characterized by its number of channels and by its noise equivalent radiance (NER). For the sake of simplicity, the bands are contiguous and cover the range 6–100 μm , because at shorter wavelengths the contribution of solar radiation cannot be neglected in daytime conditions. The spectral responses are rectangular and the bandwidths such that all bands receive the same amount of radiance at the top of atmosphere (TOA) for the Arctic winter reference case. This equienergetic partition of the channels implies that FIR bands are much wider than MIR bands (Figure 2). The reference configuration of the instrument is 10 bands, and the NER is assumed the same for each channel, equal to $0.01 \text{ W m}^{-2} \text{ sr}^{-1}$.

This is consistent with a thermal sensor

coated with gold black which has spectrally flat absorbance through the whole IR range [e.g., Ngo Phong *et al.*, 2015], and with the absence of significant spectral differences in the transmittance along the optical path. Such characteristics are expected for a grating-based or filter wheel-based radiometer. The radiometric resolution is defined in terms of NER rather than in terms of noise equivalent delta temperature (NEDT) to work at the sensor level. NEDT is helpful in comparing to actual temperature measurements, but it can be misleading as it depends on the temperature of the considered scene. Also, with this choice, increasing the number of bands clearly results in a decrease of the signal-to-noise ratio, which is easily understood because

the sensor NER remains constant, independently of the channels configuration. In the case of gratings, for instance, an increase of the spectral resolution is generally obtained at the expense of radiometric resolution. For the sake of comparison with other studies, though, Figure 2 shows the NEDT corresponding to an NER of $0.01 \text{ W m}^{-2} \text{ sr}^{-1}$ for different instrument configurations. The 20 band configuration is such that MIR NEDT is less than 0.2 K, which is similar to MODIS NEDT at 250 K. This suggests that the microbolometer-based radiometer could perform as well as MODIS sensor, except that its spectral coverage would be extended throughout the FIR.

Table 2. Spectral Bands of MODIS and TICFIRE Used in This Study^a

Band Number	MODIS	TICFIRE
1	6.8	8.7
2	7.3	11.0
3	8.6	13.0
4	9.7	17.8
5	11.0	18.5
6	12.0	19.5
7	13.4	21.5
8	13.7	25
9	13.9	40
10	14.2	-

^aThe values indicate the central wavelengths in μm .

To this end, the 10 MODIS IR channels analyzed by *Iwabuchi et al.* [2016] are used, and the NER for each channel is computed from *Xiong et al.* [2009]. The nine TICFIRE channels are defined as those of the FIRR prototype [*Libois et al.*, 2016a, Figure 2a] and cover the range 8–50 μm , and the NER is assumed to be $0.01 \text{ W m}^{-2} \text{ sr}^{-1}$ in each channel. The spectral characteristics of all these channels are detailed in Table 2. The FIRR is very similar to the Mars Climate Sounder [*McCleese et al.*, 2007] in terms of spectral coverage, and preliminary airborne and in situ measurements have highlighted the performances of this device, mak-

ing it a realistic spaceborne instrument within the next years [*Libois et al.*, 2016b]. The noise levels used for MODIS and TICFIRE remain constant throughout the paper.

2.3. Physical Motivation

Most IR cloud retrieval algorithms take advantage of spectral variations of ice and water refractive index. Figure 3a shows the imaginary parts of ice and water refractive indices. It highlights the much stronger absorption at 12 μm compared to 8 μm , which explains why in many algorithms a channel around 8 μm is used along with a channel around 12 μm . In the FIR, ice shows a unique behavior compared to liquid water. Ice absorption indeed exhibits a significant minimum around 23 μm . At this minimum, the imaginary index m_i is 2.7×10^{-2} , which is less than the value at 8.7 μm (3.7×10^{-2}). Since the ice absorption coefficient is defined as $k_i = 4\pi m_i / \lambda$, the latter is nearly 3 times lower at 23 μm than at 8.7 μm . It is also 30% less than at 3.7 μm , a critical channel to study optically thick clouds that is however affected by solar radiation in daytime conditions [*Nakajima and King*, 1990; *Platnick et al.*, 2003]. The ice refractive index spectral features determine the spectral dependence of the extinction coefficient and single-scattering albedo of ice crystals (Figures 3b and 3c). The reduced size parameter ($x = \pi d_{\text{eff}} / \lambda$) for wavelengths beyond 30 μm is responsible for a large sensitivity of the extinction efficiency and single-scattering albedo to effective diameter compared to the MIR. This makes FIR more appropriate than MIR for studying large cloud particles. In addition, the single-scattering albedo is relatively high around 23 μm and remains well above 0.5 for large particles. As a consequence, a significant amount of multiple scattering occurs in this range so that optically thick ice clouds are partly reflective and have an emissivity below 1. This drastically increases the sensitivity of emitted radiance to the effective particle diameter [*Yang et al.*, 2003], contrary to the perfect blackbody behavior observed in the MIR that hinders any information about cloud particle size. Such spectroscopic characteristic is favorable for studying cloud microphysics at the top of optically thick convective towers, for instance, where standard IR algorithms show poor performance. To some extent, the FIR contains similar information to MODIS channel centered at 3.8 μm used by *Wang et al.* [2016a], with the advantage of being unaffected by solar radiation. Note also that ice cloud optical thickness can be significantly different at 10.6, 12, 23, or 35 μm (Figure 3b). For instance, a cloud with effective particle diameter of 30 μm becomes opaque (i.e., optical thickness equals 5) at visible optical depth of 6.25 at 10.6 μm , 4 at 23 μm , and 7.63 at 35 μm . Mention of large optical thickness in the following should be considered relative to the wavelength of interest.

As shown above, the single-scattering properties of ice clouds are more sensitive to effective particle diameter in the FIR than in the MIR. The spectral signature of ice clouds at TOA does not depend only on their single-scattering properties, though. It also depends on the transparency of the atmosphere and on the total amount of radiation reaching the instrument. From the ground, the atmosphere is often opaque in the FIR range due to strong absorption by water vapor, so that FIR observations are generally disadvantaged compared to MIR observations. Largely for that reason, most studies dedicated to FIR radiation were taken in dry, cold, or elevated locations [e.g., *Turner and Mlawer*, 2010; *Shi et al.*, 2016]. On the contrary, from a satellite perspective, clouds can be observed in the FIR if the atmosphere above them is sufficiently transparent.

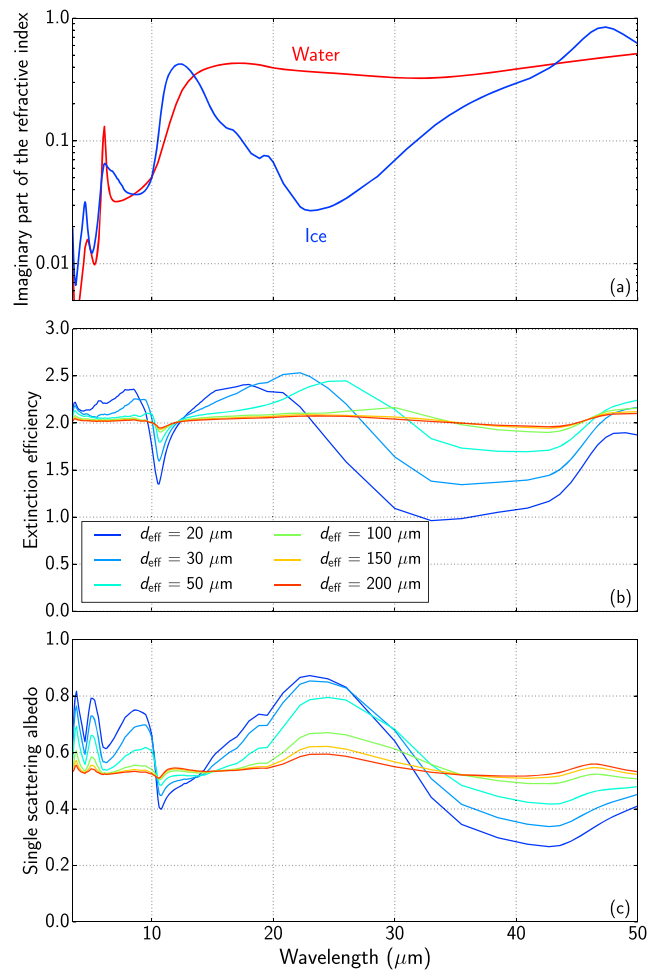


Figure 3. (a) Imaginary part of ice and water refractive indices in the range 3.5–50 μm . Spectral variations of the (b) extinction coefficient and (c) single-scattering albedo for a distribution of severely roughened column aggregates from the database of Yang et al. [2013].

Figure 4 shows the transmittance of the atmosphere above the reference clouds as a function of cloud top altitude. It shows that an ice cloud can be well observed from space up to 50 μm as soon as its top is above 5 km (10 km) for Arctic winter (tropical) conditions. These conditions are highly relevant because thin ice clouds encountered in the polar regions and tropical cirrus and convective towers often satisfy those conditions. It also shows that FIR offers an effective profiling capability throughout most of the atmosphere, by masking lower atmospheric layers and shielding the surface with increasing wavelengths in the range 17–40 μm .

2.4. Optimal Estimation Framework

2.4.1. Theoretical Framework

Generally speaking, the information content of a radiance measurement depends on its sensitivity to changes in cloud properties, on the uncertainties regarding the atmospheric state, the cloud particle size distribution and shape, and on the instrumental error. The optimal estimation method [Rodgers, 2000] accounts properly for all these contributions and has been used to assess the information content of various IR instruments such as MODIS [L'Ecuyer et al., 2006] and IASI [Rabier et al., 2002]. Since the present paper focuses on cloud radiative properties, the state vector to be retrieved only includes cloud properties. Following Wang et al. [2016a], only single-layer homogeneous clouds are considered, and the state parameter consists of the cloud top altitude h , the optical thickness τ , and the effective particle diameter d_{eff} . The cloud is assumed to be 1 km thick. All other atmospheric properties contribute to the measurement error, implying that the atmospheric state must be provided by another satellite (e.g., AIRS) or reanalysis product (e.g., ERA-Interim) [Dee et al., 2011]. Note that for hyperspectral observations, all atmospheric properties can be included in the state parameter [e.g., Merrelli and Turner, 2013].

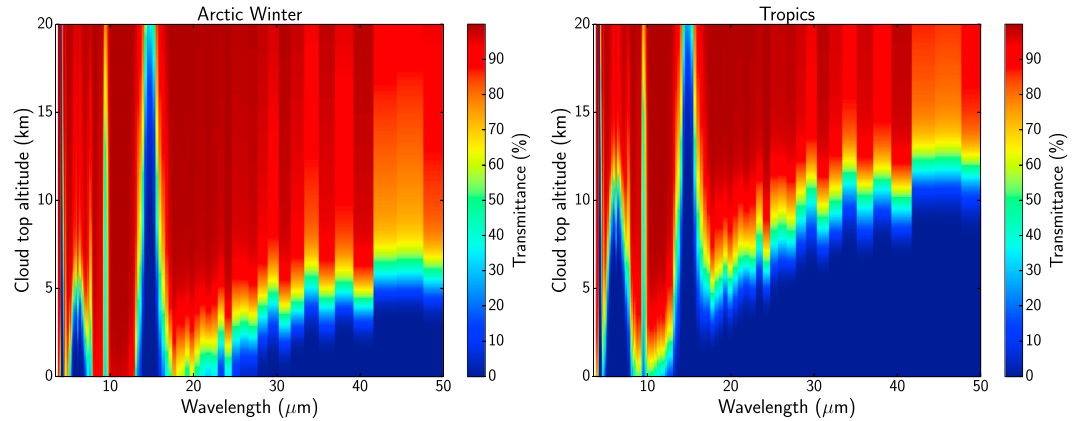


Figure 4. Simulated spectral atmospheric transmittance between the top of a cloud and the TOA as a function of cloud top altitude, for Arctic winter and tropical conditions. The simulations were performed at 15 cm^{-1} spectral resolution.

The optimal estimation framework can be written as follows:

$$\mathbf{y} = \mathbf{F}(\mathbf{x}^t, T_s^t, \epsilon_s^t, \mathbf{T}^t, \mathbf{RH}^t, H^t) + \epsilon^{\text{obs}}, \quad (1)$$

where \mathbf{y} is the observation vector, \mathbf{F} the forward model that returns the TOA radiances as a function of all atmospheric information, and ϵ^{obs} the observation error. The superscript t indicates the true state, which means that the forward model is assumed perfect. This is consistent with the results of Wang *et al.* [2016a] who showed that model errors are much smaller than other contributions. Besides the state vector \mathbf{x} , the simulated TOA radiance depends on surface temperature T_s , surface spectral emissivity ϵ_s , temperature and relative humidity profiles \mathbf{T} and \mathbf{RH} , and ice habit H including actual habit and particle size distribution. Since the true parameters are unknown, the simulated radiance computed from a best estimate of the atmospheric state deviates from the true radiance, so that equation (1) can be rewritten as

$$\mathbf{y} = \mathbf{F}(\mathbf{x}^t, T_s, \epsilon_s, \mathbf{T}, \mathbf{RH}, H) + \epsilon^{T_s} + \epsilon^{\epsilon_s} + \epsilon^{\mathbf{T}} + \epsilon^{\mathbf{RH}} + \epsilon^H + \epsilon^{\text{obs}}, \quad (2)$$

$$\mathbf{y} = \mathbf{F}(\mathbf{x}^t, \mathbf{p}) + \epsilon^y, \quad (3)$$

where the measurement error ϵ^y is the sum of errors $\epsilon^i = \frac{\partial \mathbf{F}}{\partial p_i} (p_i - p_i^t)$, ϵ^H , and ϵ^{obs} , and \mathbf{p} the parameter vector including all ancillary parameters p_i . The optimal estimation method aims at determining the posterior distribution of \mathbf{x}^t given an a priori on \mathbf{x} and a set of observations. The quantity to be retrieved is thus $P(\mathbf{x}^t | \mathbf{y})$. According to Bayes' theorem,

$$P(\mathbf{x}^t | \mathbf{y}) = \frac{P(\mathbf{y} | \mathbf{x}^t) P(\mathbf{x}^t)}{P(\mathbf{y})}. \quad (4)$$

For the sake of simplicity, it is assumed that all probability density functions are Gaussian. Although this is a strong assumption, it is very widely used, especially in data assimilation, due to the resulting easiness of implementation. In this case,

$$\ln(P(\mathbf{y} | \mathbf{x}^t)) = [\mathbf{y} - \mathbf{F}(\mathbf{x}^t, \mathbf{p})]^T \mathbf{S}_y^{-1} [\mathbf{y} - \mathbf{F}(\mathbf{x}^t, \mathbf{p})] + c_1, \quad (5)$$

$$\ln(P(\mathbf{x}^t)) = [\mathbf{x}^t - \mathbf{x}^a]^T \mathbf{S}_a^{-1} [\mathbf{x}^t - \mathbf{x}^a] + c_2, \quad (6)$$

where \mathbf{S}_y is the error covariance matrix corresponding to the errors ϵ^y , \mathbf{x}^a the a priori state parameter, and \mathbf{S}_a its associated error covariance, and the subscript T indicates transposition. \mathbf{S}_a is such that the a priori uncertainties on h is 4 km, and τ and d_{eff} are known within a factor of 10 and 5, respectively; c_1 and c_2 are constants. From equation (4),

$$\ln(P(\mathbf{x}^t | \mathbf{y})) = [\mathbf{y} - \mathbf{F}(\mathbf{x}^t, \mathbf{p})]^T \mathbf{S}_y^{-1} [\mathbf{y} - \mathbf{F}(\mathbf{x}^t, \mathbf{p})] + [\mathbf{x}^t - \mathbf{x}^a]^T \mathbf{S}_a^{-1} [\mathbf{x}^t - \mathbf{x}^a] + c_3. \quad (7)$$

It can be shown [Rodgers, 2000] that the posterior distribution $P(\mathbf{x}^t|\mathbf{y})$ is then defined as a multivariate Gaussian distribution with mean \mathbf{x}^p and error covariance matrix \mathbf{S}_p such that

$$\ln (P(\mathbf{x}^t|\mathbf{y})) = [\mathbf{x}^t - \mathbf{x}^p]^\top \mathbf{S}_p^{-1} [\mathbf{x}^t - \mathbf{x}^p] + c_0, \quad (8)$$

$$\mathbf{S}_p = \left(\mathbf{S}_a^{-1} + \mathbf{K}_x^\top \mathbf{S}_y^{-1} \mathbf{K}_x \right)^{-1}. \quad (9)$$

The matrix \mathbf{K}_x contains the derivatives of the TOA radiance with regard to the state parameters, also called the Jacobians:

$$\mathbf{K}_x = \left[\frac{\partial \mathbf{F}}{\partial h}, \frac{\partial \mathbf{F}}{\partial \tau}, \frac{\partial \mathbf{F}}{\partial d_{\text{eff}}} \right]. \quad (10)$$

The state \mathbf{x}^{opt} that maximizes $P(\mathbf{x}^t|\mathbf{y})$ is the maximum likelihood estimation. For retrieval applications it can be estimated using the Gauss-Newton algorithm [Rodgers, 2000]. This iterative method is such that the state \mathbf{x}_{n+1} at step $n+1$ is determined from the state \mathbf{x}_n at step n by

$$\mathbf{x}_{n+1} = \mathbf{x}^a + \left(\mathbf{S}_a^{-1} + \mathbf{K}_n^\top \mathbf{S}_{y,n}^{-1} \mathbf{K}_n \right)^{-1} \mathbf{K}_n^\top \mathbf{S}_{y,n}^{-1} [\mathbf{y} - \mathbf{F}(\mathbf{x}_n) + \mathbf{K}_n (\mathbf{x}_n - \mathbf{x}^a)], \quad (11)$$

where the Jacobians and error covariance matrices are computed at each step n .

2.4.2. Measurement Error Contributions

In this study, three independent sources of errors are considered: (1) observation error, (2) uncertainties on the surface and atmospheric states, and (3) uncertainties on crystal habit and particle size distribution. All the error sources are assumed independent, and the global error covariance matrix \mathbf{S}_y is simply the sum of all the individual contributions. Uncertainties in trace gases concentrations, though potentially critical for channels overlapping CO_2 or O_3 absorption bands, are not considered here. All radiative transfer calculations are performed with MODTRAN v.5.4 [Berk et al., 2005] using the correlated- k method. Multiple scattering is accounted for using DISORT [Stamnes et al., 1988] with 16 streams. The water vapor continuum is computed from the MT-CKD 2.5 parameterization [Clough et al., 2005]. The spectral surface emissivities are taken from Feldman et al. [2014]. For the Arctic winter case, it is assumed that the surface is snow covered, while for the tropical case, it is ocean water.

For the observation error, the instrument NER is assumed similar in each band, equal to $0.01 \text{ W m}^{-2} \text{ sr}^{-1}$. This is consistent with the laboratory characterization of the FIRR [Libois et al., 2016a] when averaging the signal over a 2-D array of uncooled microbolometers. Although such NER is not yet achieved for a FIR imaging system, it is expected that improved optical and electronic design should allow to meet this target within a few years. The absence of any window on the optical path in space will also be beneficial to the response of the instrument, contrary to ground operation in which the FIRR detector works under vacuum in a sealed package. Observation errors in distinct channels are assumed uncorrelated, so that the error covariance matrix \mathbf{S}_{obs} is diagonal.

Uncertainties on surface emissivity, surface skin temperature, and temperature and humidity profiles, altogether referred to as ancillary parameters, also affect the quality of the retrieval. Here we assumed that the surface emissivity uncertainties in each band are uncorrelated and equal to 0.01. Such errors correspond to the imperfect knowledge of surface emissivity in the FIR, not to a mischaracterization of the surface which would result in larger and correlated errors [Feldman et al., 2014]. This implies that such values hold only when the type of surface is well known. Surface temperature uncertainty is taken as 0.5 K. The errors on the temperature and humidity profiles are 1 K and 15% at each level. These errors are vertically correlated in an exponential way such that correlation vanishes at 1 km distance. Such values, also used by Wang et al. [2016a], are consistent with the accuracy of state-of-the art reanalysis products or IR sounders atmospheric products. The prior and measurement uncertainties used in the study are summarized in Table 3. The case of larger uncertainties for the atmospheric and surface parameters, which might be more realistic for the Arctic, is discussed in section 4. The derivatives of TOA radiance with respect to the ancillary parameters are computed with MODTRAN using finite differences [e.g., Garand et al., 2001] to convert the above mentioned errors into measurement errors (equation (2)). These measurement errors depend on cloud characteristics and are thus computed for each individual scene.

Studies dedicated to the MIR generally neglect the impact of particle size distribution, because it was shown to induce smaller uncertainties than crystal habit [e.g., Cooper et al., 2006]. Although this is true for the MIR,

Table 3. Uncertainties for the Prior State Parameters, for the Ancillary Parameters, and for the Radiance Measurements Used Throughout the Study^a

Quantity	$\ln \tau$	$\ln d_{\text{eff}}$	h	T_s	ϵ_s	T	RH	Radiance
Uncertainty (nominal)	$\ln 10$	$\ln 5$	4 km	0.5 K	0.01	1 K	15%	0.01 W m^{-2}
Uncertainty (high)	-	-	-	2 K	0.03	2 K	25%	-

^aThe high values are used in section 4.2.

it is not the case in the FIR where particle size distribution can have an impact similar to crystal habit [Baran, 2007]. As a consequence, it is included in the present error analysis because both habit and size distribution uncertainties can result in changes of TOA radiance close to 5% in FIR bands. To account for those uncertainties, several simulations were performed for various habits and size distributions. Practically, the nine habits of the database of Yang *et al.* [2013] are used, with the three investigated roughness parameters. Size distributions are assumed to follow a modified-gamma distribution [e.g., Petty and Huang, 2011; Merrelli and Turner, 2013] with effective variances 0.1 or 0.2. For each cloud scene, 54 simulations are thus performed, and the error covariance matrix \mathbf{S}_{hab} is computed from these simulations.

2.4.3. Information Content

The information content of a set of observations is estimated through Shannon information content (SIC), which quantifies the entropy reduction of the state parameter resulting from the observations. Here SIC is defined as

$$\text{SIC} = \frac{1}{2} \ln \left| \mathbf{S}_o \mathbf{S}_p^{-1} \right|. \quad (12)$$

This quantity can be used to compare the information content of observations taken either with different instruments or with a particular set of channels. For instance, it has been used to select the most informative channels of IASI [Rabier *et al.*, 2002], which are currently assimilated in numerical weather forecast models or to identify the most informative channels of MODIS [Cooper *et al.*, 2006; Wang *et al.*, 2016a]. In addition to SIC, the retrieval uncertainty for each state parameter is defined as the square root of the diagonal elements of \mathbf{S}_p .

3. Results

3.1. Jacobians of TOA Radiance

The Jacobians of TOA radiance in terms of the state parameters were computed for both Arctic and tropical atmospheres. They are shown in Figure 5 as a function of cloud optical thickness. Since the bandwidths were selected to equipartition the amount of energy available in each band for the reference Arctic winter case, the energy partition slightly varies with optical thickness. As a consequence, for large optical depth, the amount of energy available in FIR bands exceeds that available in MIR bands, because the cloud scene becomes colder and Planck emission spectrum is shifted toward the FIR. For the same reason, the energy available in FIR bands is similar for the Arctic and tropical reference cases, because FIR channels probe the higher troposphere, which temperature is similar in the Arctic and tropics. On the contrary, MIR observations are greatly advantaged at low optical depth in the tropics because they are sensitive to the high emission of the warm surface. Fortunately, FIR observations do not suffer the disadvantage of MIR observations in cold regions. More generally, the thermal contrast between the surface and the cloud is much larger in the MIR, making MIR observations more sensitive to small changes of optical thickness in warm regions.

The most striking point in Figure 5 is the high sensitivity of FIR TOA radiance to changes in d_{eff} for the Arctic case. Indeed, while MIR sensitivity is relatively low and completely vanishes at optical thickness above 10, the sensitivity around $23 \mu\text{m}$ is much larger and increases with optical thickness. This intrinsic advantage of the FIR results from the larger sensitivity of cloud single-scattering properties to effective diameter highlighted in Figure 3. The small differences of single-scattering albedo are amplified through multiple scattering, so that the advantage increases with optical thickness. When clouds become perfectly opaque to surface radiation, their signature only comes from cloud emission. As in the MIR, thick clouds are nearly blackbody emitters; their signature is independent of d_{eff} . In the FIR, on the contrary, because clouds have emissivity less than one, their signature still carries information about particle size. This is very similar to clouds characteristics at $3.7 \mu\text{m}$ [Wang *et al.*, 2016a] or in the visible [Nakajima and King, 1990]. For the tropical case, FIR channels are

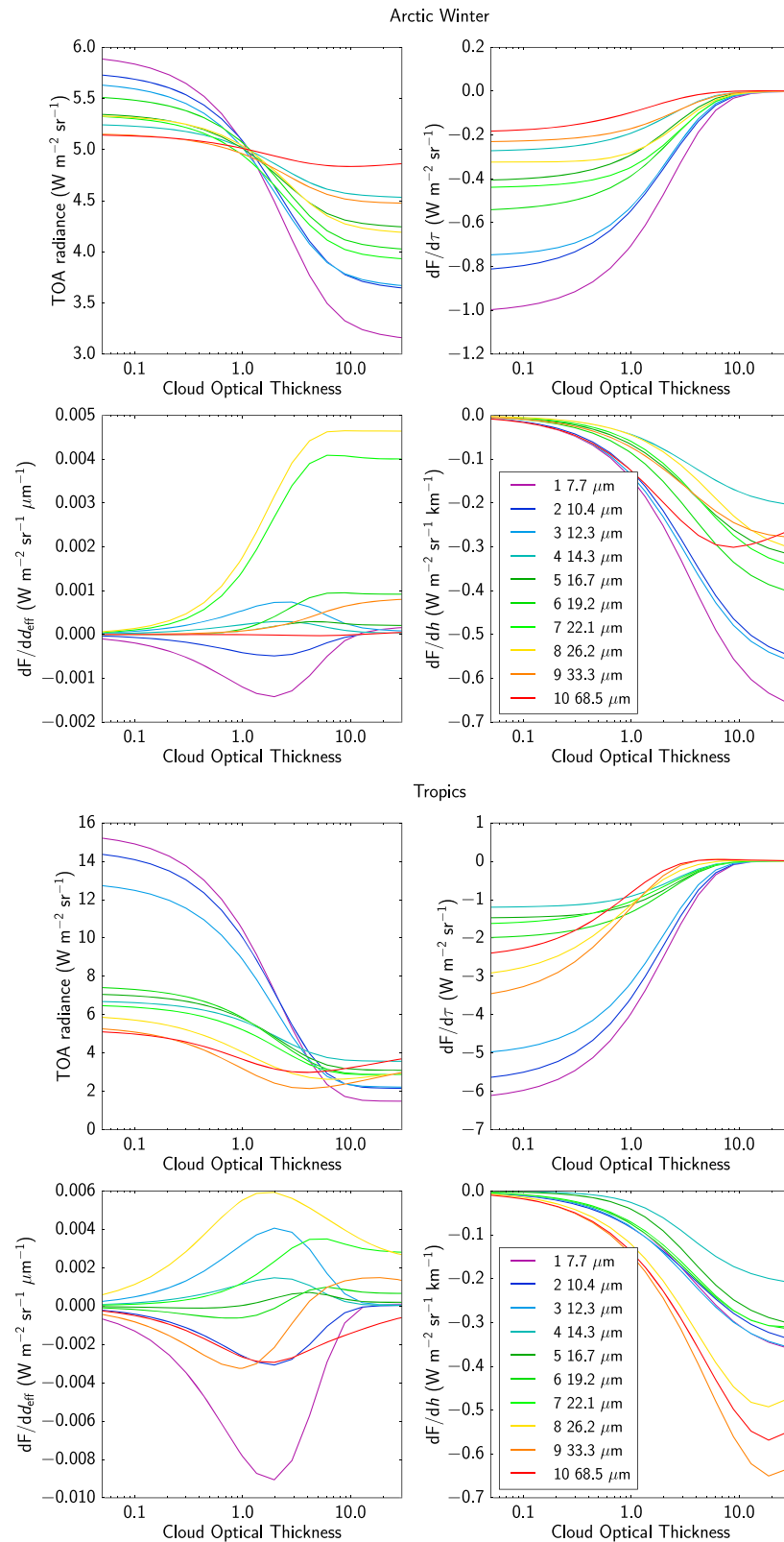


Figure 5. Jacobians of TOA radiance with respect to cloud state parameters for the Arctic winter and tropical atmospheres. Both clouds consist of severely roughened column aggregates with effective diameter 60 μm following a modified gamma distribution with effective variance 0.1. The Arctic winter cloud is located between 5 and 6 km, and the tropical cloud is between 14 and 15 km.

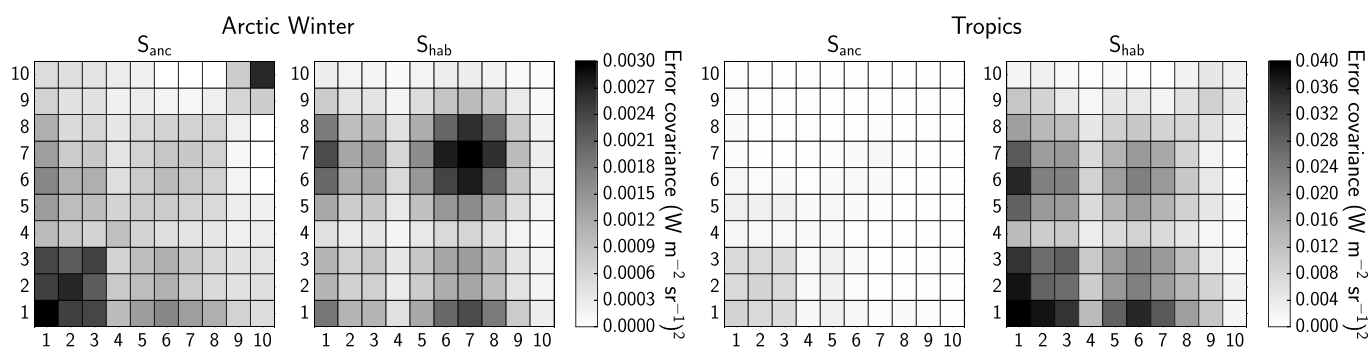


Figure 6. Error covariance matrices of the ancillary parameters (S_{anc}) and crystal habit (S_{hab}) for both reference cases. The numbers correspond to the spectral bands as follows: 1: 7.7 μm ; 2: 10.4 μm ; 3: 12.3 μm ; 4: 14.3 μm ; 5: 16.7 μm ; 6: 19.2 μm ; 7: 22.1 μm ; 8: 26.2 μm ; 9: 33.3 μm ; 10: 68.5 μm .

mainly advantaged at large optical thickness. At small optical thickness, the smaller sensitivity of MIR channels to d_{eff} is compensated by the larger thermal contrast between the surface and the extremely cold cloud. This shows that FIR observations can be extremely useful to observe cloud microphysics at the top of optically thick convective towers, for instance [Jensen et al., 1996]. Using FIR channels overall offers a way to overcome the natural limit of MIR algorithms at large optical thickness [Iwabuchi et al., 2016].

3.2. Error Covariance Matrices

The error contributions of ancillary parameters and crystal habit for the two reference cases are shown in Figure 6. Observation errors are not shown because they are much smaller. For the Arctic case, uncertainties on surface temperature and emissivity have a strong impact because the atmosphere is very transparent. They impact more MIR channels, which are more sensitive to the surface than FIR channels. FIR channels are mostly affected by water vapor uncertainties above the cloud. Crystal habit induces the largest errors in the weakly absorbing channels of the FIR, because multiple scattering amplifies small differences in single-scattering properties. This large uncertainty is nevertheless compensated by the advantageous sensitivity to d_{eff} displayed in Figure 5. Crystal habit impact is less in the MIR, because single-scattering properties are less dependent to crystal habit. For the tropical cloud, errors on ancillary data do not impact much the global error because surface emission barely reaches the top of the atmosphere in such wet conditions, and because errors on temperature and humidity profiles below the cloud are largely attenuated by the cloud. Regarding crystal habit, its absolute impact is larger in the MIR because the amount of radiation in these bands is almost 3 times more than in the FIR (Figure 5). However, the relative uncertainty in simulated radiances due to crystal habit uncertainties remains much larger in the FIR than in the MIR.

These uncertainties are propagated to the retrieved state of the atmosphere through the optimal estimation method. To estimate the contribution of each error source to the total uncertainty of the retrieved state parameters, the posterior uncertainty is first computed, accounting for all the sources and then a single source contribution is removed. The contribution of the removed source is defined as the difference. Those contributions are shown in Figure 7 for both reference cases. It shows that, in general, observation errors are minor, except for the determination of d_{eff} in the Arctic. More generally, observation uncertainties are more critical in the Arctic because of the lower signal-to-noise ratio. In the Arctic, h and τ retrievals mainly depend on ancillary parameter uncertainties, while in the tropical case, ice habit is critical as well because most of the signal comes from the cloud, not from the atmosphere below.

3.3. Information Content Analysis

The information content of a set of observations is assessed through SIC (section 2.4.3). For a given atmospheric configuration, this quantity is used to select channels containing most information in a decreasing order. The first channel selected is that which contains, alone, most information. The second channel is that of the remaining channels, which when added to the first selected, adds up most of the remaining information, and so on. Each time a new channel is added, the total information content increases and the uncertainties on the state parameters decrease. Figure 8 shows the progressive decrease of the uncertainties as the number of channels used increases, for the two reference cases. In both cases, the first selected channel essentially constrains the optical thickness. Thereafter only are cloud top altitude and effective particle diameter are constrained. Interestingly, although the first channel selected is in the MIR, the next two are in the FIR. In the tropical case, channels 2 to 5 are in the FIR. It should also be noted that most information is captured with

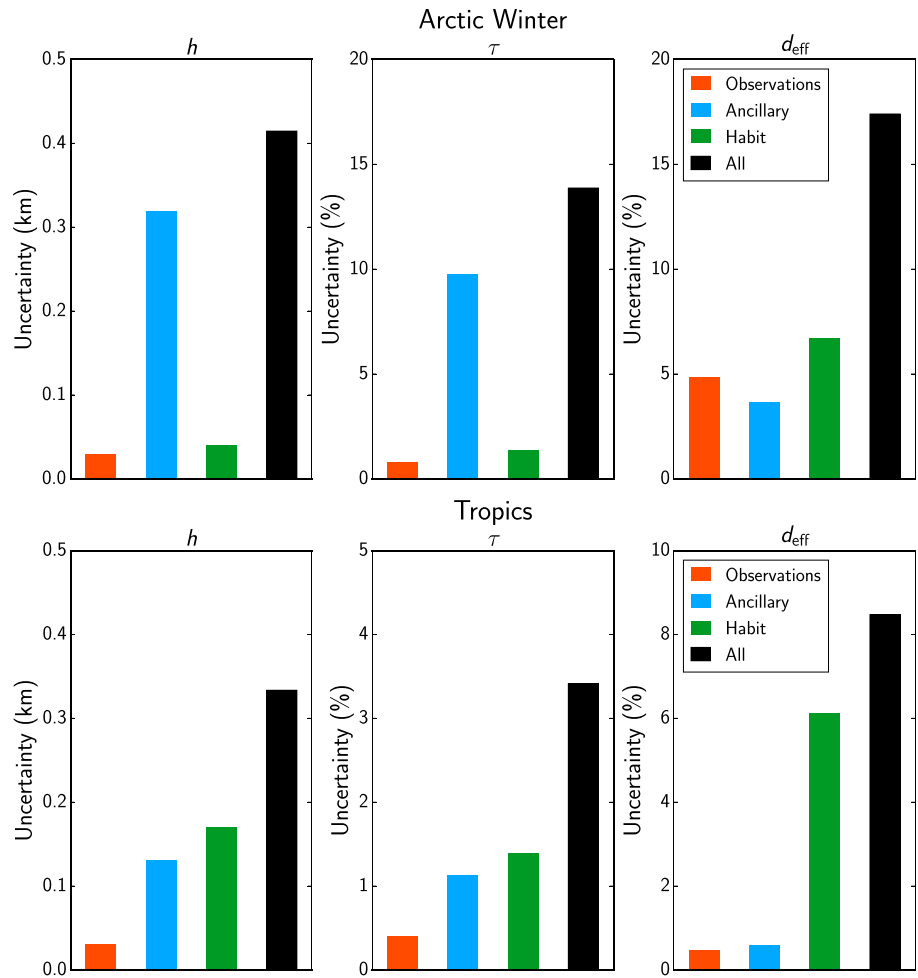


Figure 7. Contributions of the error sources to the total posterior uncertainties, when MIR and FIR channels are used. Each source contribution is obtained by computing the difference between the total posterior uncertainties and the uncertainties when this source is removed.

only five channels, the reduction in uncertainty beyond five channels being marginal. This is consistent with the findings of Wang et al. [2016a]. Regarding the degree of uncertainty, cloud top altitude can be estimated within about ± 400 m. Optical thickness and effective diameter can be retrieved within approximately 15% to 20% error for the Arctic case, and within less than 10% error in the tropical case.

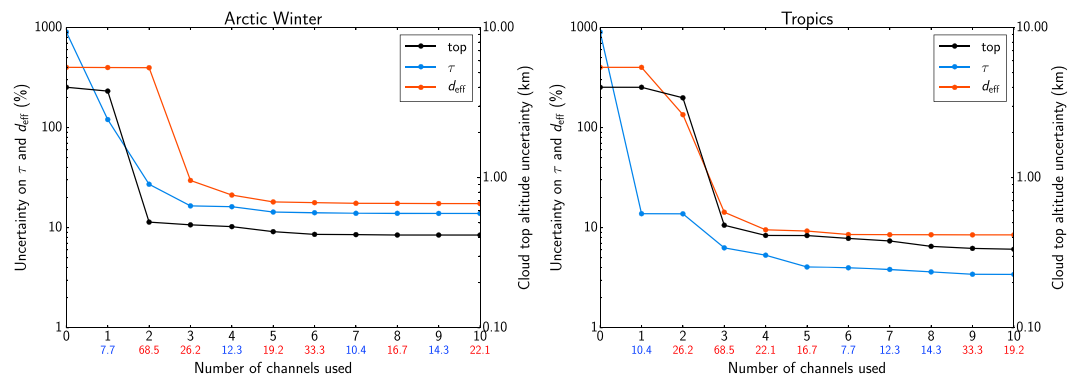


Figure 8. Decrease of state parameters uncertainties as the number of observations increases. The numbers below the graphs indicate the central wavelengths of the selected channels. Blue refers to MIR channels while red indicates FIR channels.

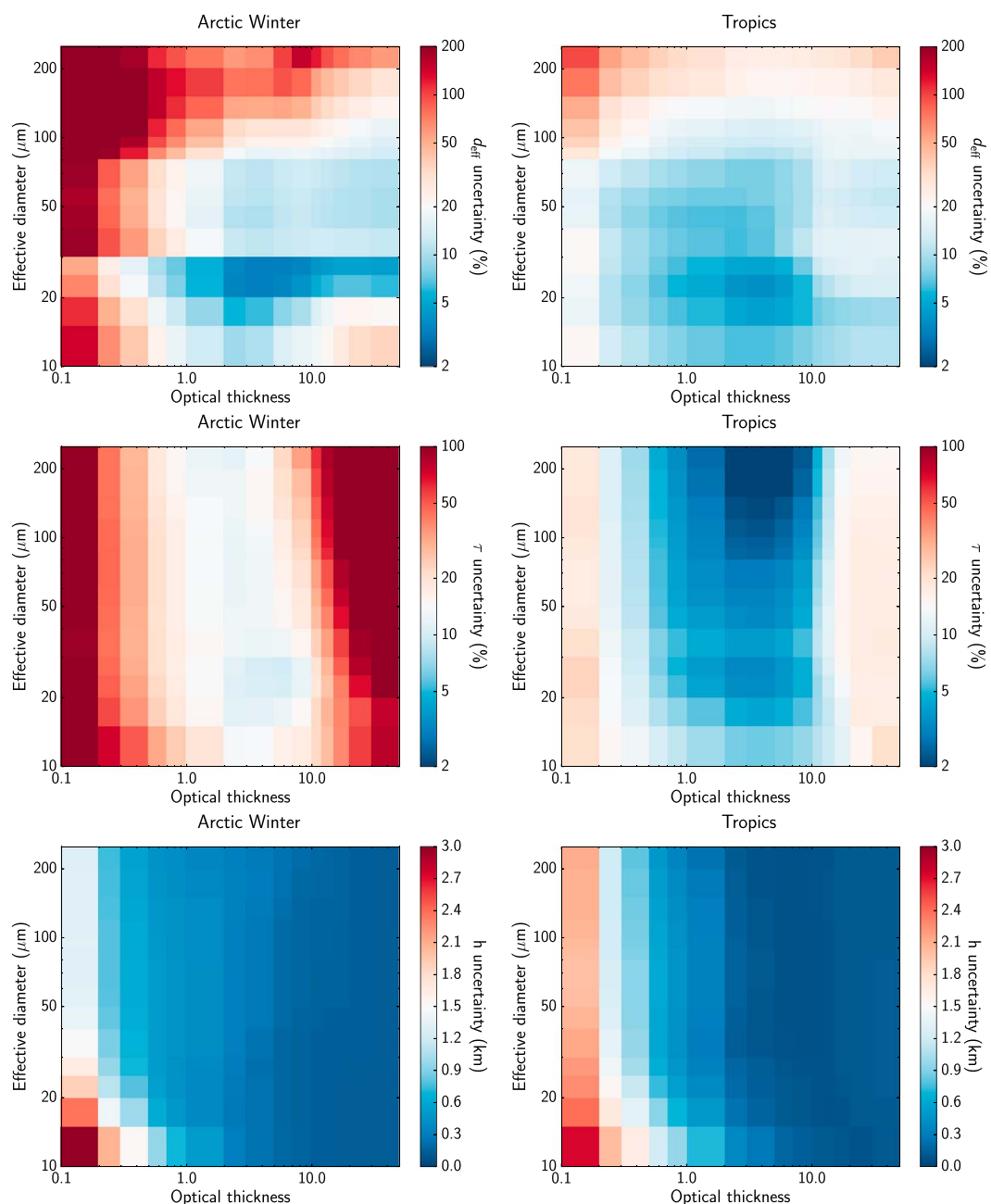


Figure 9. Uncertainties on h , τ , and d_{eff} after all channels of the 10-band synthetic radiometer have been used, for a wide range of cloud optical thickness and effective particle diameter.

These uncertainties illustrate two particular cases. To explore how they change as a function of cloud characteristics, the same method was applied to various combinations of cloud thickness and effective particle diameter. The resulting uncertainties are shown in Figure 9. In general, errors for the Arctic case are larger than those for the tropics. The noise level of the instrument being fixed, the signal-to-noise ratio is indeed lower in the Arctic because the emitted radiation from the colder scene is lower. The effective particle diameter retrieval performs best for optical thickness above 1 and for effective diameter up to approximately 150 μm . This is likely to extend the potential of MIR radiometry that generally performs poorly for optical thickness larger than 5 and effective diameter exceeding 100 μm . The retrievals of optical thickness are best for intermediate optical thickness ($1.0 < \tau < 10$) but are also very efficient in the tropics for optically thin and optically thick clouds. Cloud top altitude is very well constrained, except for very thin clouds. Errors on d_{eff} are often below 15%, making it possible to distinguish without ambiguity small particles from large particles.

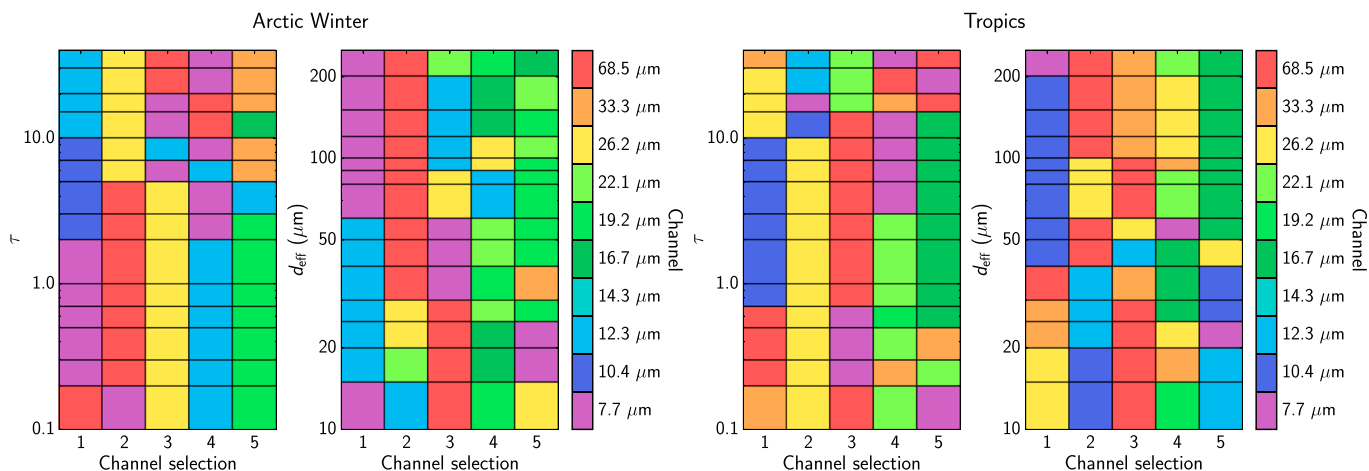


Figure 10. Identification of the five most informative channels (in decreasing order of importance), when (left) cloud optical thickness or (right) effective particle diameter are varied from the reference cases.

Figure 10 shows the five most informative channels for both reference cases, when optical thickness and effective diameter are varied from the reference state. The channels 26.2 and 68.5 μm often appear in the first positions, which can be explained by the large amount of information they contain about cloud top and effective diameter. In most situations it remains necessary to use at least one MIR channel because it constrains well the optical thickness in the atmospheric window. Note also that some channels have less importance and are seldom selected. This suggests that removing channels 14.3, 19.2, and 33.3 μm would not degrade the performance of the radiometer. Such considerations should be borne in mind when designing a new instrument.

4. Discussion

4.1. Added Value of FIR Observations

It was shown that FIR observations are most useful when the thermal contrast between the cloud and the surface is low, when the cloud is opaque in the MIR, and when the atmosphere above the cloud is sufficiently transparent to let cloud emission escape to TOA. The former conditions are encountered when cloud optical thickness is large or when the surface is cold. This makes FIR observations very valuable to probe polar ice clouds and optically thick high-altitude ice clouds in general. Although the potential of FIR radiometry has been shown in terms of absolute retrieval performances (Figure 9), it is worth quantifying the added value relative to MIR-only observations. To this end, the method detailed in section 3.3 was applied to a synthetic radiometer made of only the first four MIR bands of the 10-band synthetic radiometer. The relative decrease in d_{eff} uncertainty resulting from the addition of the six FIR channels is presented in Figure 11. As expected, in both Arctic and tropical cases, the largest improvement is for optical thickness beyond 10, because those are the conditions where FIR observations are most sensitive to d_{eff} , contrasting with the inherent limitations of MIR observations in such cases. In those cases, the uncertainty is reduced by more than 80%. The improvement is very significant for intermediate optical thickness ($\tau = 0.5 - 5$) as well, often exceeding 50%. This is particularly true for the Arctic case which is inherently disadvantaged with MIR alone due to the low radiance emitted by the cold surface. At small optical thickness, the uncertainty is barely reduced for the Arctic case. On the contrary, it is largely reduced in the tropical case because the thermal contrast between the surface and the cloud is larger, and the cloud emission in the FIR is unaltered by water vapor absorption above. This highlights the strong potential of FIR observations for studying optically very thin cirrus clouds, especially for large ice crystals ($d_{\text{eff}} > 50\mu\text{m}$). To some extent, using FIR observations adds a new retrieval capability for thick clouds and large particles in cases without reflected solar radiation.

Adding FIR channels not only reduces the uncertainties of the retrieved cloud properties but also reduces the correlations between the retrieved state variables. Table 4 shows these correlations ρ for both reference cases, when only MIR channels are used and when all channels are used. Adding FIR channels reduces all the correlated errors and is most useful to discriminate between h and d_{eff} .

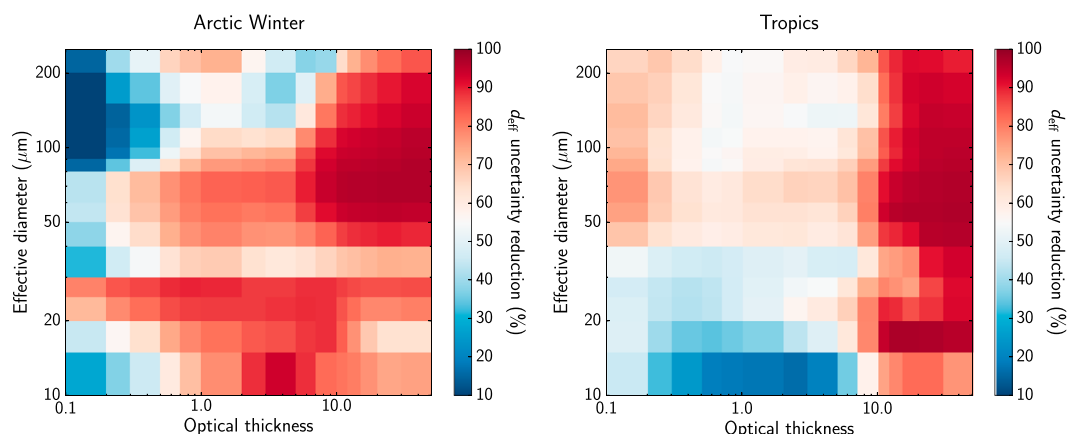


Figure 11. Relative decrease in d_{eff} uncertainty resulting from the addition of six FIR channels to four MIR channels, for Arctic winter and tropical conditions.

So far, the obtained results are theoretical because the instrument which they refer to does not exist yet. To give it a more realistic flavor, the same method was applied to the real instruments described in section 2.2. For this, the added value of the future TICFIRE satellite was quantified with regard to MODIS (see section 2.2). Figure 12 is similar to Figure 11 except that the reference corresponds to the 10 bands of MODIS, and the full instrument corresponds to MODIS channels complemented by the nine channels of TICFIRE. The patterns for the effective particle diameter are very similar to those of Figure 11. The values are slightly lower, though, because the 10 channels of MODIS contain more information than the four MIR channels of the synthetic radiometer. The largest difference is the more limited improvement for cloud particles beyond 100 μm in the tropical case. The reductions in uncertainty for optical thickness and cloud top altitude are also shown for the Arctic case. FIR observations help constrain all cloud parameters for a large variety of cloud characteristics. They also reduce the correlated errors of the retrieved parameters (Table 4). The reductions in uncertainty for cloud top altitude and optical thickness in the tropical case are not shown since they are not as significant as in the Arctic case. These results overall highlight that adding TICFIRE observations to existing MODIS observations would greatly increase the performance of cloud properties retrieval algorithms in the polar regions and also for thin cirrus and convective ice clouds in the tropics [Hong et al., 2007].

The added value of FIR observations is further illustrated in Figure 13 (similar to Figure 8), showing how using TICFIRE observations reduce the uncertainties on cloud properties for a thin and a thick Arctic cloud. It suggests that adding two or three FIR channels to MODIS would drastically improve cloud retrieval performance. Practically, this could be done at reasonable cost by adding such a FIR radiometer on the A-Train or Earth-CARE orbit [Illingworth et al., 2015]. Alternatively, it suggests that a compact radiometer such as TICFIRE, which covers the MIR and the FIR, could entirely replace MODIS for ice cloud monitoring.

4.2. Range of Validity of the Algorithm

All previous results are bound to the assumed uncertainties of the ancillary parameters. Those were chosen to be consistent with the work of Wang et al. [2016a] but may be optimistic, especially for the polar regions where a priori atmospheric profiles are generally poorly constrained. To estimate the sensitivity of the results to the

Table 4. Correlations Between the Retrieved State Parameters for the Two Reference Cases, When MIR-Only or MIR and FIR Channels Are Used^a

	Arctic Winter		Tropics	
	MIR	MIR + FIR	MIR	MIR + FIR
$\rho_{\ln \tau, \ln d_{\text{eff}}}$	-0.88 (-0.65)	-0.13 (-0.02)	-0.56 (-0.43)	-0.41 (-0.56)
$\rho_{\ln \tau, h}$	-0.97 (-0.97)	-0.67 (-0.49)	-0.87 (-0.60)	-0.31 (-0.15)
$\rho_{\ln d_{\text{eff}}, h}$	0.87 (0.67)	-0.016 (0.06)	0.54 (0.30)	-0.20 (-0.06)

^aThe quantities in parenthesis indicate the correlated errors when MODIS-only or MODIS and TICFIRE channels are used.

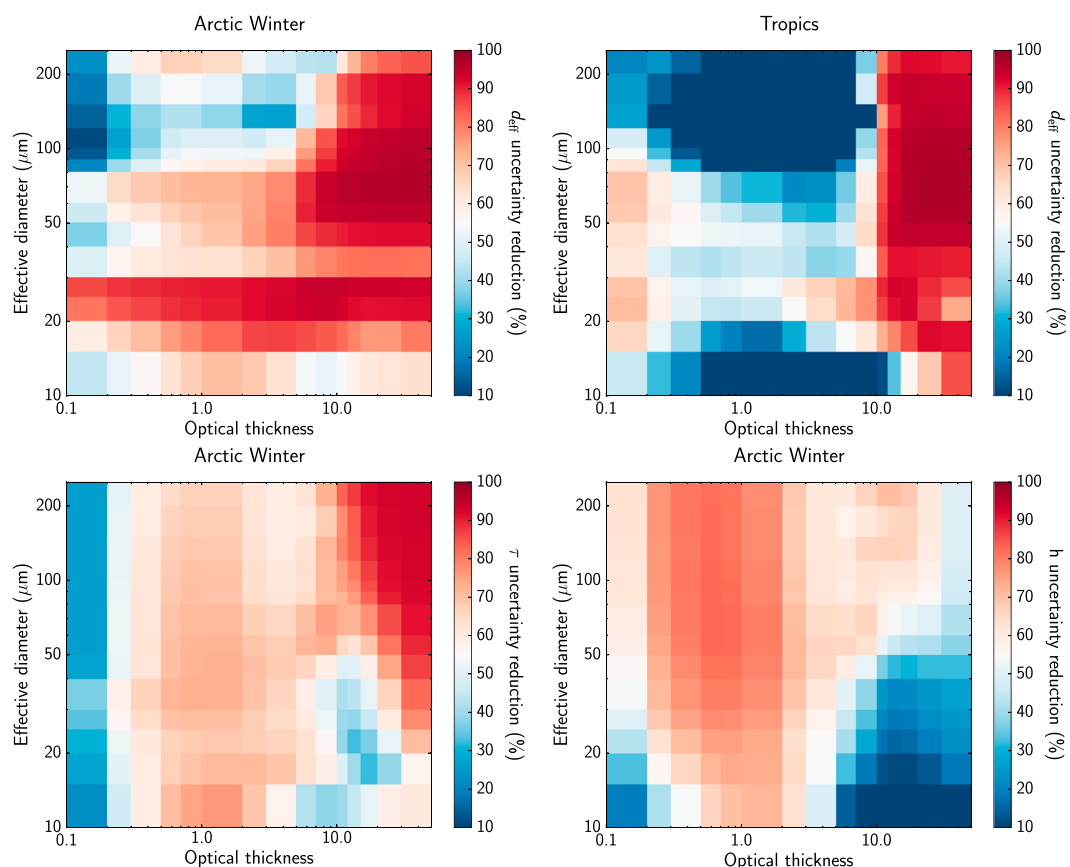


Figure 12. (top row) Relative decrease in d_{eff} uncertainty resulting from the addition of the nine TICFIRE channels to 10 MODIS channels, for Arctic winter and tropical conditions. (bottom row) Relative decrease in τ and h uncertainties resulting from the addition of the nine TICFIRE channels to 10 MODIS channels for the Arctic winter atmosphere.

ancillary parameter uncertainties, each individual uncertainty was varied individually, all other things being constant. The impact of such variations on the posterior uncertainties for both reference cases are shown in Figure 14. For the Arctic case, h retrieval is mostly sensitive to the temperature profile and τ retrieval also depends on the surface temperature. The posterior error of d_{eff} is very sensitive to errors on surface emissivity, because FIR channels that mostly constrain d_{eff} also see the surface. This highlights that surface properties should be well determined to operate the algorithm. It is critical in the Arctic when open leads are present in the scene but ignored by the algorithm, since water and snow have very distinct emissivities in the FIR [Feldman et al., 2014]. The impact of such surface heterogeneities, though crucial, is not further investigated here. In the tropics, all error sources have a similar impact on the retrievals, but the sensitivity is much less than in the Arctic, mostly because the cloud is high and the surface contribution to the TOA radiance is limited due to atmospheric absorption below the cloud. These results show that the algorithm remains efficient even when the ancillary parameters are poorly constrained. In addition to this sensitivity study, Figure 15 shows the uncertainty reduction due to the addition of TICFIRE channels to MODIS channels for large uncertainties on the surface temperature, surface emissivities, and thermodynamical profiles, in agreement with the values chosen by Wang et al. [2016a] (Table 3). The added value of FIR channels is generally reduced compared to the case with better constrained ancillary parameters, but the uncertainty reduction on d_{eff} slightly increases in the tropics.

The added value of FIR observations for the retrieval of ice cloud properties has been demonstrated for ideal cloud geometries, but it is worth discussing the impact of cloud heterogeneities on retrieval performances. A FIR radiometer is likely to have a spatial footprint much larger than current MIR radiometers. Although the resolution of the TICFIRE instrument is not known so far (it will depend on the field of view, the number of pixels of the detector, the number of filters, the acquisition rate, etc.), it should be around 10 km. In comparison,

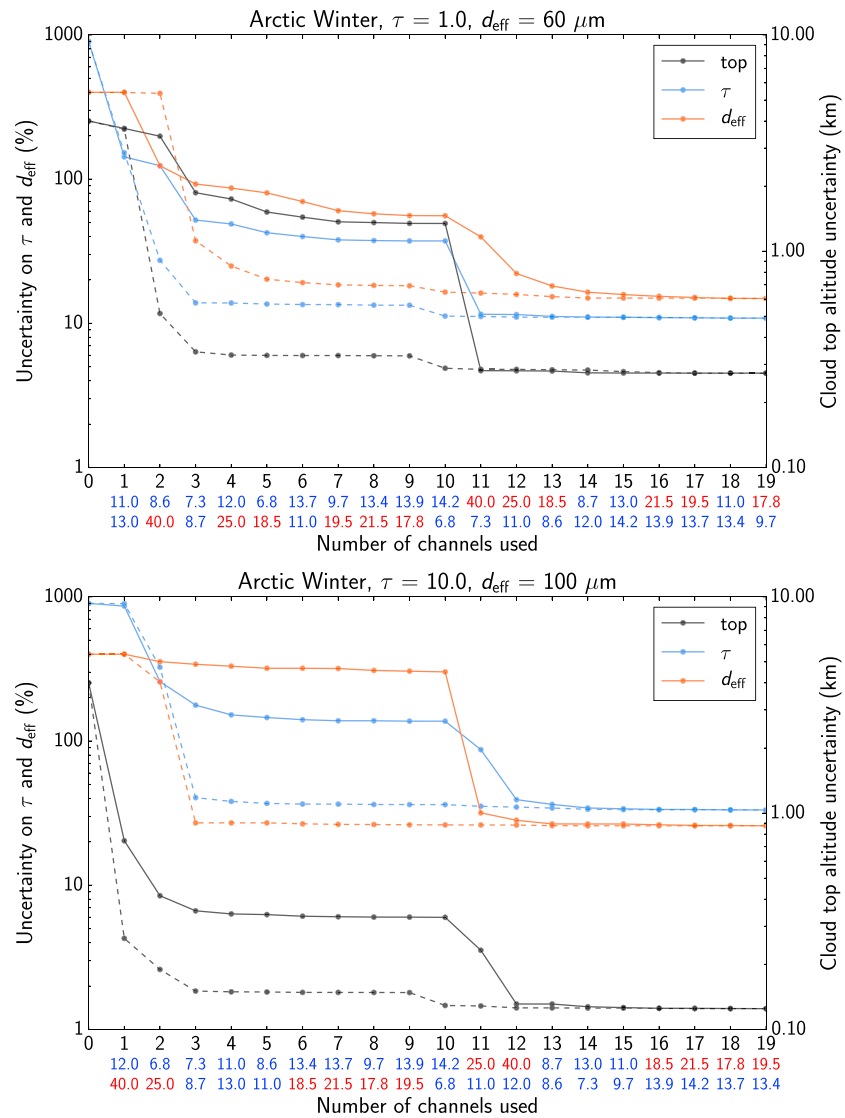


Figure 13. Reduction of cloud properties uncertainties as the number of combined MODIS and TICFIRE observations increases. The plain lines correspond to the case when the 10 MODIS channels are taken first, and then the nine TICFIRE channels are added. The dashed lines correspond to the case when TICFIRE channels are used first. The numbers below the graphs indicate the central wavelengths of MODIS and TICFIRE channels. The first (respectively second) row corresponds to the plain (respectively dashed) lines. Blue refers to MIR channels while red indicates FIR channels. Note that the TICFIRE instrument has three MIR channels and six FIR channels.

MODIS footprint is around 1 km. As a consequence, the comparison of MIR and FIR information content should properly account for these differences in spatial resolution. Since this is beyond the scope of the present paper, the current results are most valid for large-scale homogeneous cloud systems. Such systems, as observed in the Arctic polar night [Grenier et al., 2009], are the main target of TICFIRE at synoptic scales.

The impact of cloud heterogeneity was nevertheless estimated in a simple way, by treating cloud fraction as an ancillary parameter. Figure 16 shows the error covariance matrices associated to an actual cloud fraction of 0.95 instead of 1. They are compared to the other error contributions. In the Arctic, assuming that a pixel is entirely filled with clouds when it contains 5% of clear sky results in errors similar to the uncertainties associated to the temperature profile. In the tropics, small errors on cloud fraction are very critical in the MIR due to the strong thermal contrast between the surface and the cloud. Generally, it means that for cloud fraction less than 0.9, assuming the pixel is overcast might be the largest source of error of the retrieval. Practically, an operational algorithm should rely on independent sources for cloud cover.

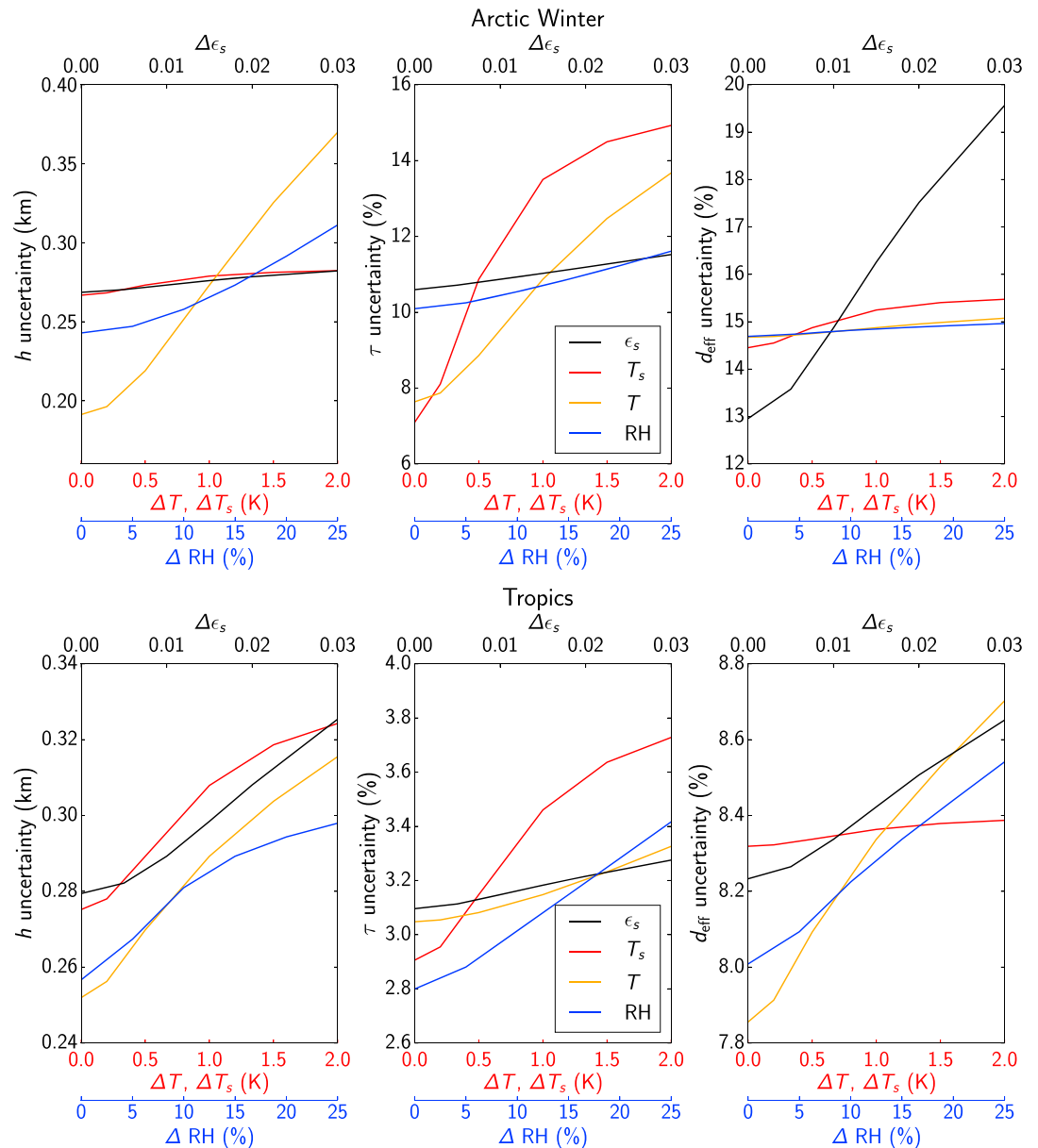


Figure 14. Variations of the posterior state parameters uncertainties as a function of the ancillary parameter errors for the two reference cases. When the uncertainty of one parameter is varied, all others are maintained at their nominal values (see Table 3).

All these uncertainties were obtained in the case of a homogeneous single-layer cloud. Multilayer cloud systems or subpixel horizontal heterogeneities, which are not accounted for by our 1-D radiative transfer computations, are likely to degrade the quality of the retrieval [Fauchez et al., 2015; Wang et al., 2016b]. Accounting for 3-D effects, in general, in remote sensing is a challenging issue but essential to improve current algorithms [e.g., Schäfer et al., 2016]. The potential of FIR radiometry for studying multilayer systems should be explored. The spectral variations of water vapor absorption in the FIR are such that some channels may see only the highest clouds while others would sense the whole column. Likewise, FIR could be valuable to study the vertical structure of clouds, which is essential to better understand ice cloud microphysics.

4.3. Sensitivity to Instrument Radiometric Resolution

The previous results were obtained assuming a NER of $0.01 \text{ W m}^{-2} \text{ sr}^{-1}$ for the FIR synthetic radiometer. Although the contribution of the measurement error is minor in the total error budget (Figure 6), it is worth investigating its impact on the retrieval performance and could provide quantitative targets to the industry

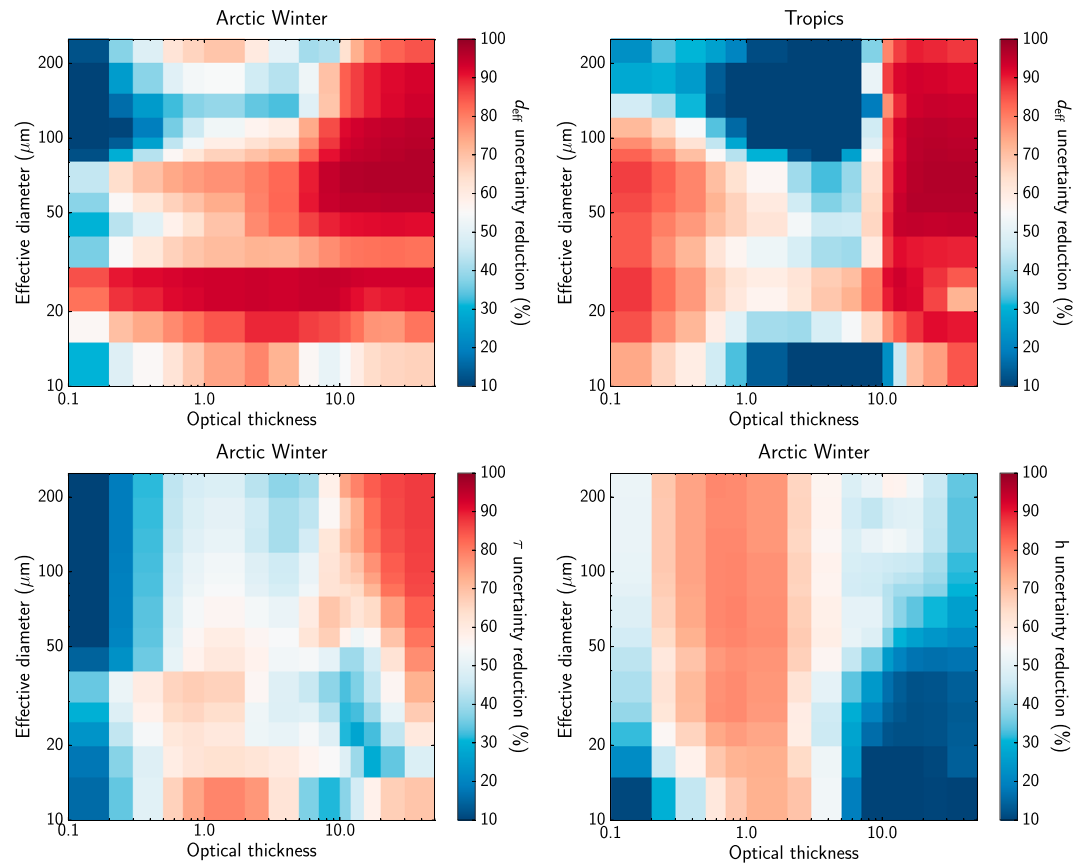


Figure 15. Same as Figure 12, except that the uncertainties on the ancillary parameters are larger (see Table 3).

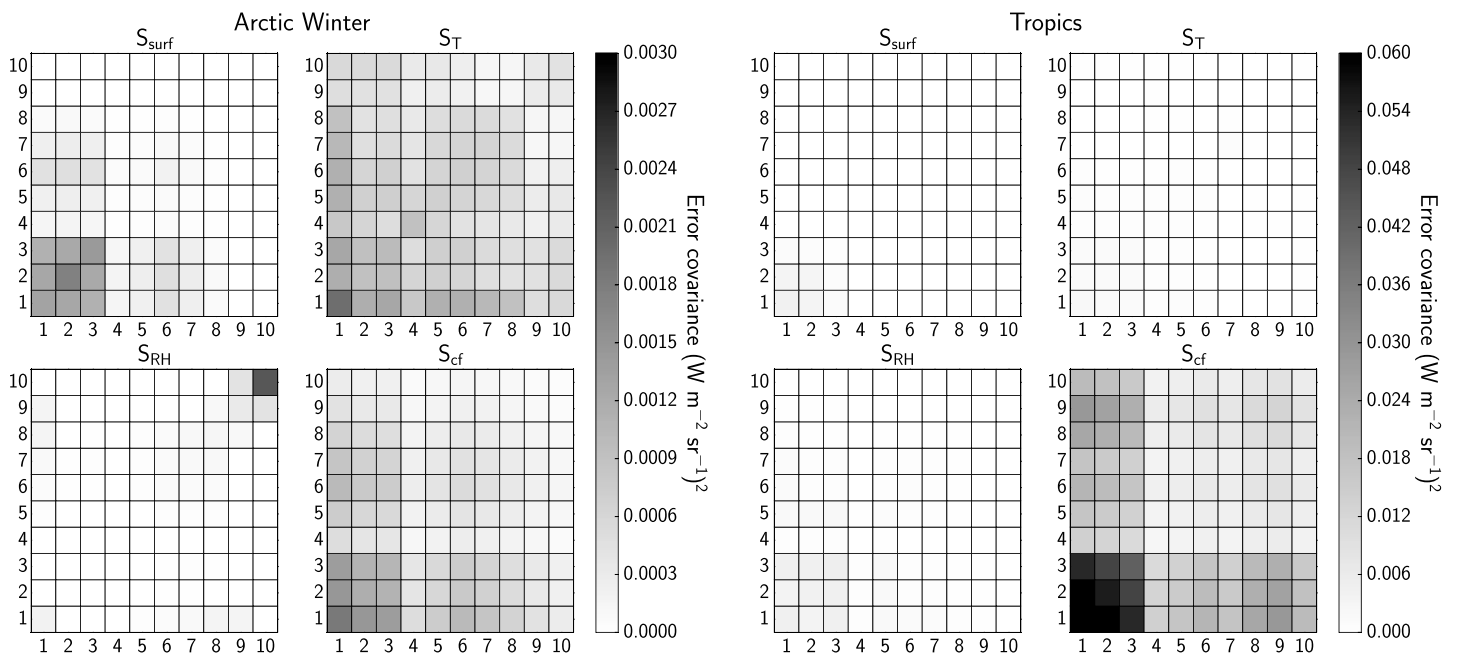


Figure 16. Error covariance matrices associated to the ancillary parameters (S_{surf} , S_T , and S_{RH}) and to the uncertainty on cloud fraction (S_{cf}) for both reference cases. S_{surf} is the sum of the surface emissivity and surface temperature errors. The numbers correspond to the spectral bands as follows: 1: 7.7 μm ; 2: 10.4 μm ; 3: 12.3 μm ; 4: 14.3 μm ; 5: 16.7 μm ; 6: 19.2 μm ; 7: 22.1 μm ; 8: 26.2 μm ; 9: 33.3 μm ; 10: 68.5 μm .

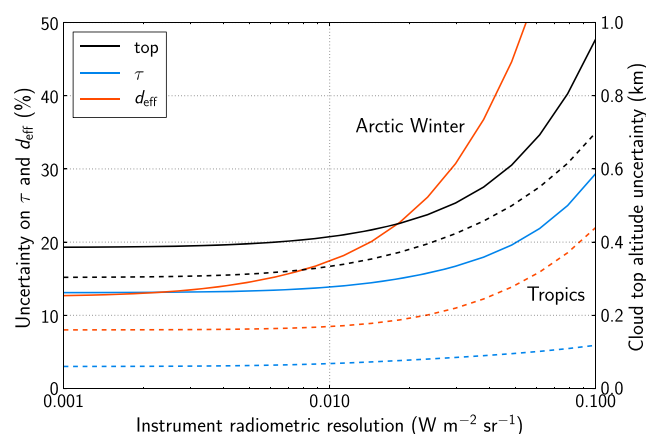


Figure 17. Variations of cloud retrieval uncertainties as a function of instrument radiometric resolution, for the two reference cases. The plain lines correspond to the Arctic winter case, and the dashed lines to the tropical case.

in view of meeting scientific requirements requested by the geophysical community. Figure 17 shows the variations of the uncertainties for both reference cases as a function of instrument radiometric resolution. It demonstrates that the retrieval uncertainties in the Arctic case significantly increase when the radiometric resolution exceeds $0.02 \text{ W m}^{-2} \text{ sr}^{-1}$. On the contrary, upgrading the resolution to $0.001 \text{ W m}^{-2} \text{ sr}^{-1}$ does not significantly reduce the retrieval uncertainties. The tropical case is less sensitive to sensor noise because the signal-to-noise ratio is favorable in a warmer atmosphere. This suggests that the selected resolution of $0.01 \text{ W m}^{-2} \text{ sr}^{-1}$ provides a good trade-off between realistically achievable technology and retrieval performance. A radiometric resolution worse than $0.03 \text{ W m}^{-2} \text{ sr}^{-1}$ would be damageable for the quality of the retrieval, and efforts are highly recommended to exceed this target.

4.4. Sensitivity to the Number of Channels

The results presented so far were mostly based on the 10-band configuration of the synthetic FIR radiometer. Although it suggests that approximately five bands contain the bulk of the information, it is worth exploring the dependence of the performance on the total number of bands of the radiometer. Using thinner bands, for instance, may help select the regions of the spectrum where sensitivity is maximal and where uncertainties due to ancillary parameters are minimal. Too narrow bands may however suffer a low signal-to-noise ratio. Figure 18a shows how SIC varies with an increasing number of contiguous bands. The increase is significant up to approximately seven channels, but limited for additional channels. The small oscillations observed beyond five channels suggest that an optimal configuration could be degraded by increasing the number of bands due to a spectral shift of those optimal bands. Practically, it suggests that an instrument with around seven channels would be sufficient. The gain in information content resulting from increasing the number of channels would certainly come at the expense of acquisition rate, effective spatial resolution, technical complexity, and cost, which has to be considered beforehand. Such statement is worthy in view of designing a FIR radiometer dedicated to ice cloud observation.

These results also imply that instruments with a large number of bands could be optimized by merging adjacent bands in order to increase the signal-to-noise ratio. Such considerations could be applied in the case of hyperspectral measurements. Instead of using a limited number of channels for data assimilation [e.g., Rabier *et al.*, 2002], merging channels could, for instance, result in improved performances without increasing computing time since the effective number of assimilated observations would remain constant. More generally, this points out that instruments dedicated to clouds observation do not require very high spectral resolution. Most recent FIR satellite projects focused on such high spectral resolution, though, because they also aim at providing information about atmospheric profiles and trace gases [e.g., Merrelli and Turner, 2012].

Although four to five channels are generally sufficient to provide most of the information, these very channels depend on the scene [Cooper *et al.*, 2006]. Here the most useful channels in the 10-band configuration are chosen as follows. For each (τ, d_{eff}) configuration illustrated in Figure 9, a channel is assigned its rank of selection. Then the sum of all these values is computed for each channel and those with the minimal values are the most informative. For the Arctic winter cases, the four most valuable channels are (in decreasing order of importance) 12.3, 7.7, 68.5, and 26.2 μm . For the tropical cases, those are the 26.2, 68.5, 33.3, and 10.4 μm . For the combination of both atmospheres, the most informative channels are the 68.5, 26.2, 12.3, and 7.7 μm . This highlights the necessity of using FIR channels.

From the previous analysis, the number of useful bands was estimated to be less than 10. Since these actual bands were defined only on the basis of equienergetic partition (section 2.2), we now investigate what would

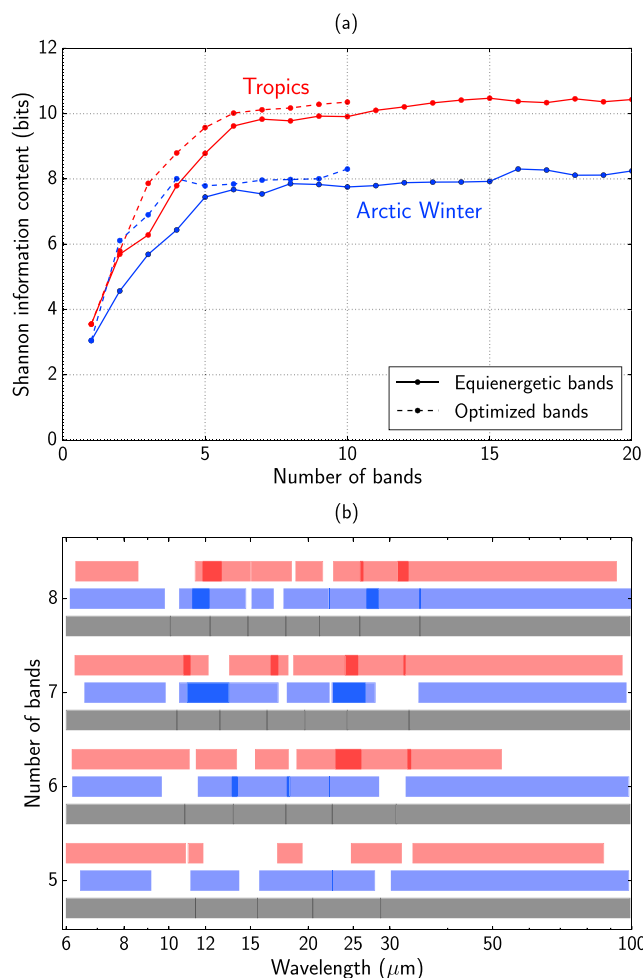


Figure 18. (a) Shannon information content of the observations as a function of the total number of bands, for the two reference cases. The plain lines correspond to equienergetic bands, while the dotted lines correspond to optimized bands. (b) Spectral characteristics of the equienergetic and optimized bands for the Arctic (blue) and tropical (red) reference cases, for the 5-, 6-, 7-, and 8-band configurations.

be the ideal set of channels for a given number of bands. For this, the channels edges are varied from the reference equienergetic configuration. A minimization tool (SciPy [Jones et al., 2001] *fmin* function) is used to find the configuration that maximizes the information content for each number of bands. This configuration is obtained after 300 iterations of the minimization algorithm. The dashed lines in Figure 18a show the information content as a function of band numbers for these optimized channels. Although there is no guarantee that the obtained optimized bands correspond to a global optimum, it highlights that a significant amount of information can be gained by choosing appropriately the positions and bandwidths of each band, once the number of channels has been imposed. For instance, using six optimized channels for the tropical case is equivalent to using 11 equienergetic channels. These optimized channels are shown in Figure 18b for the reference cases. It demonstrates that choosing overlapping channels can improve performances, as excluding parts of the spectrum can do by removing segments of the spectrum responsible for increasing uncertainties. These conclusions hold for systems where the amount of available energy in one band is independent of the other bands, as is the case for filter-wheel systems acquiring sequentially in time the different bands. In a system where all spectral channels are acquired simultaneously, though,

overlapping would imply that energy is split in multiple bands, which would reduce the signal-to-noise ratio and potentially degrade the overall information content.

4.5. Retrieval Performance

The present study only focused on the information content of the radiance measurements, without explicitly performing cloud properties retrievals. As in the studies of Cooper et al. [2006] and Merrelli and Turner [2013], the uncertainties obtained for cloud parameters are thus theoretical and bound to the assumptions underlying the optimal estimation method, in particular, that all considered errors are unbiased and Gaussian. Practically, departure from this ideal behavior can result in bias that the present theory does not account for [Wang et al., 2016b]. Only the computation of retrievals can assess the actual performance of the method. Although this is beyond the scope of this paper, a retrieval has been applied for the Arctic winter atmosphere, with a representative cloud situated between 5.0 and 6.0 km, of optical thickness 2.7 and effective diameter 76 μm. For this profile, 20 synthetic FIR radiometer measurements were computed from the true expected measurements, by adding a white Gaussian noise corresponding to a radiometric error of 0.01 W m⁻² sr⁻¹. For each measurement, the Gauss-Newton algorithm detailed in section 2.4.1 was applied, starting from an a priori \mathbf{x}^0 that is relatively far from the true state ($h = 8$ km, $\tau = 1.0$, and $d_{\text{eff}} = 40$ μm). The iterations are stopped

when the difference between two consecutive states or the deviation from the observations is sufficiently small, or when the number of steps reaches 15.

For this particular case, the average retrieved values of h , τ , and d_{eff} are 6.0 km, 2.6, and 77 μm , respectively. The standard deviations among the 10 measurements are 60 m, 0.1, and 9 μm . This end-to-end simulation highlights the very good performance of the retrieval for this particular example. It is characterized by nearly no bias, and standard deviations even better than the 1 sigma uncertainties expected from the optimal estimation framework, namely, 290 m, 0.34, and 12 μm . The obtained correlated errors ($\rho_{\ln \tau, \ln d_{\text{eff}}} = -0.64$, $\rho_{\ln \tau, h} = -0.63$, and $\rho_{\ln d_{\text{eff}}, h} = 0.48$) are similar to those expected from the optimal estimation ($\rho_{\ln \tau, \ln d_{\text{eff}}} = -0.34$, $\rho_{\ln \tau, h} = -0.71$, and $\rho_{\ln d_{\text{eff}}, h} = 0.1$) except for h and $\ln d_{\text{eff}}$. For an exhaustive validation of the algorithm, the retrieval should nevertheless be applied to a variety of atmospheric conditions and cloud altitudes as in Wang *et al.* [2016b]. To perform such exercise, and in view of the development of an operational retrieval product, a faster radiative transfer code is recommended, such as those presented in Wang *et al.* [2016a] or Yi *et al.* [2016].

5. Conclusion

This paper investigated the potential of FIR radiometry for the characterization of ice cloud properties, with a special focus on cloud effective particle diameter. To this end we used the optimal estimation framework, which provides the best estimate of cloud properties and the associated uncertainties given an a priori and a set of radiance observations. It was shown that in the polar regions and the upper tropical troposphere, FIR radiances contain much more information about cloud effective particle diameter than MIR radiances. This results from the advantageous spectral shift of Planck emission function in cold conditions and from the strong sensitivity of cloud particle single-scattering properties to effective diameter in the FIR. Using FIR observations could thus overcome the limitations of common MIR-based algorithms, increasing retrievals accuracy by more than 50% in most cases, and by nearly 100% in some conditions. This would extend the range of validity of existing algorithms to larger optical thickness, larger effective diameter, and to the polar regions in absence of sunlight, thus offering the possibility to observe the initiation of precipitation. Such advancements are promising for studying the microphysics of convective towers and poorly known polar thin ice clouds, which are known to be sensitive to anthropogenic influence through ice nucleation processes. Practically, the performance of existing FIR sensors are such that a radiometer with 2 or 3 FIR channels would be sufficient to significantly complement MIR observations. Increasing sensor radiometric resolution could provide another twofold in precision, and optimizing the channels spectral characteristics appears as another venue to improve retrieval performance. Future work should focus on the assessment of FIR-based retrievals, exploring a larger range of cloud cases. This could be done by coupling a FIR radiometer simulator to outputs of reanalysis or regional climate simulations. In summary, this work highlights the relevance of adding FIR observations to the existing Earth-observing system. Such FIR satellite is technologically feasible and highly recommended. In addition, it could be performed at a reasonable cost compared to projects involving high spectral resolution instruments.

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